



Introduction to Nested Functions (smod_t2/t3)



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Outline

- Introduction
- Why use Nested Functions?
 - Reasons
 - Uses
 - Disadvantages
- Behaviour in *smod_t2/3*
- Production systems
 - Price & Quantity Systems
- Method
- Exercises and Experiments



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Introduction

- Model *smod_t* - ‘state-of-the-art’ c1980s
- *smod_t2*
 - ‘state-of-the-art’ c1990s
 - 2 level production nest
- *smod_t3*
 - ‘state-of-the-art’ c2010s
 - 3 level production nest
- Databases (SAMs)
 - Aggregates of regions (*smod_t*)
 - Less aggregated SAMs

Many ‘modern’ models are not ‘state-of-the-art’ c2024

***smod_t3*: a model that provides a framework that can be augmented to produce a model that is ‘state-of-the-art’ c 2015**



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Why Use Nested Functions?



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Reasons for Nested Functions

- Enhanced representation of economic systems
- Allow different substitution possibilities between ‘groups’ of inputs
 - Capital and aggregate labour
 - ‘Skilled’ and ‘unskilled’ labour
 - Land and ‘fertiliser’
 - Capital and aggregate energy
 - etc....

“when used in equilibrium modelling applications, traditional flexible functional forms suffer from an excess of flexibility”
(Perroni and Rutherford, 1995, p 336)

Nested CES functions “provide a second-order local approximation to any cost function if and only if the function to be approximated is globally regular”. (Perroni and Rutherford, 1995, p 336)

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Uses of Nested Functions

- **Production**
 - ‘Standard’ models, e.g., aggregates of different ‘groups’ of factors (usually labour types)
 - ‘Energy’ models, e.g., aggregates of different energy inputs
 - Agriculture focused models, e.g., aggregates of land/fertiliser/phytosanitary inputs
 - Climate change/IAM models, e.g., ‘energy’ models plus emissions plus
 - Water models, e.g., potable water/irrigation water, etc...
- **Trade**
 - Multiple trade partners, e.g., global CGE models
- **Consumption**
 - Aggregates of different ‘groups’ of commodities, e.g., substitution between types of food
 - Labour-Leisure trade-offs
 - Substitution between commodities produced within and without the SNA production boundary

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Disadvantages of Nested Functions

- How much nesting is the appropriate amount of nesting?
 - Economic logic
 - KISS
- Where do we get estimates of the substitution elasticities?
 - Little empirical evidence
 - Sensitivity analyses

"Essentially, all models are wrong, but some are useful" (G Box)



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Behaviour



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Social Accounting Matrix

	cagr	cnres	cmanu	cserv	aagr	anres	amanu	aserv	fnd	fuskl	fsklb	fcap	h_urban	h_rural	imptax	exptax	saltax	prodtax	dirtax	Govt	i_s	row	total
cagr	0	0	0	0	31	0	52	9	0	0	0	0	136	44	0	0	0	0	0	0	3	22	297
cnres	0	0	0	0	0	7	86	1	0	0	0	0	1	0	0	0	0	0	0	0	0	219	315
cmanu	0	0	0	0	36	36	356	171	0	0	0	0	271	109	0	0	0	0	0	7	190	143	1,318
cserv	0	0	0	0	25	33	174	201	0	0	0	0	219	105	0	0	0	0	0	178	19	62	1,016
aagr	276	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	276
anres	0	291	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	291
amanu	0	0	930	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	930
aserv	0	0	0	935	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	935
fnd	0	0	0	0	24	66	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	90
fuskl	0	0	0	0	110	17	93	156	0	0	0	0	0	0	0	0	0	0	0	0	0	0	375
fsklb	0	0	0	0	1	3	19	116	0	0	0	0	0	0	0	0	0	0	0	0	0	0	139
fcap	0	0	0	0	45	123	134	258	0	0	0	0	0	0	0	0	0	0	0	0	0	0	559
h_urban	0	0	0	0	0	0	0	0	57	307	112	222	0	0	0	0	0	0	0	0	0	0	698
h_rural	0	0	0	0	0	0	0	0	33	68	27	176	0	0	0	0	0	0	0	0	0	0	304
imptax	6	1	54	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	61
exptax	0	1	2	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	3
saltax	1	0	33	8	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	42
prodtax	0	0	0	0	5	7	17	23	0	0	0	0	0	0	0	0	0	0	0	0	0	0	51
dirtax	0	0	0	0	0	0	0	0	0	0	0	0	20	16	0	0	0	0	0	0	0	0	36
Govt	0	0	0	0	0	0	0	0	0	0	0	0	0	0	61	3	42	51	36	0	0	0	193
i_s	0	0	0	0	0	0	0	0	0	0	0	0	162	51	29	0	0	0	0	0	8	0	212
row	14	22	299	73	276	291	930	935	90	375	139	559	698	304	61	3	42	51	36	193	212	408	
total	297	315	1,318	1,016	276	291	930	935	90	375	139	559	698	304	61	3	42	51	36	193	212	408	

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Behaviour: from smod_t

- Trade with ROW (rest of world)
 - Imports
 - Armington insight (CES)
 - Exports
 - Symmetrical treatment to imports (CET)
 - Current Account balance
 - Exchange rate- Household
 - Stone-Geary (LES) utility functions
- Government
 - Fixed real shares of government income
- Taxes
 - Import duties; export; GST; Production; Income
- Investment
 - Fixed real shares of savings

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Behaviour: Production

- smod_t2
 - Two-level production nest
 - Aggregate intermediate & ‘primary’ inputs
 - Leontief or CES
 - Aggregate ‘primary’ inputs
 - CES
- smod_t3
 - Three-level production nest
 - Aggregate intermediate & ‘primary’ inputs
 - Leontief or CES
 - Aggregate ‘natural’ and aggregate ‘primary’ inputs
 - CES
 - Aggregate ‘natural’ ‘primary’ inputs
 - CES



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Production Systems



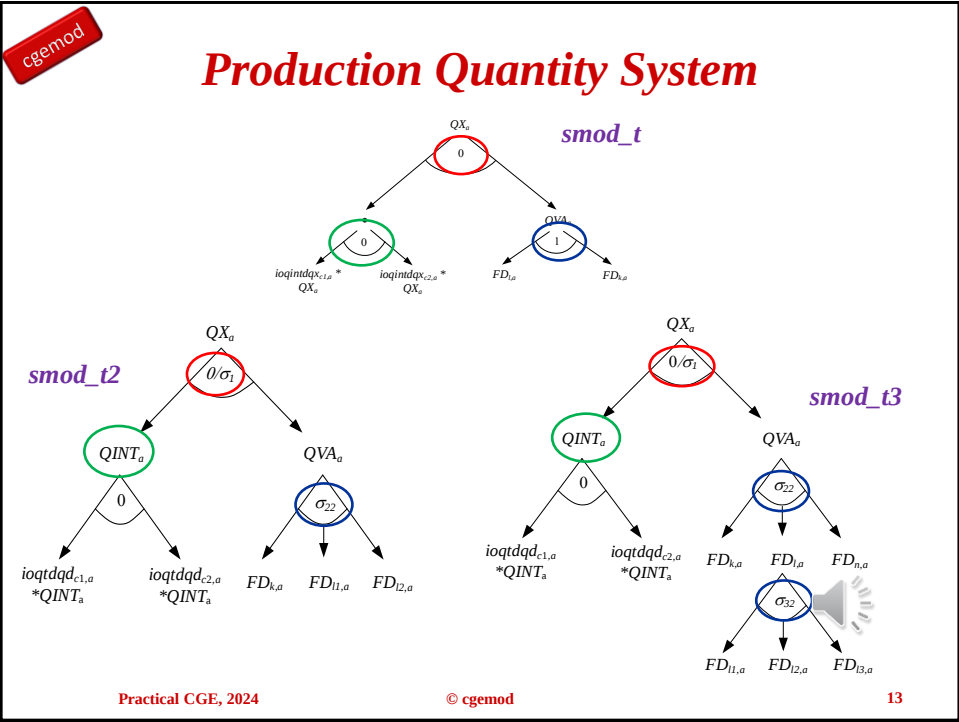
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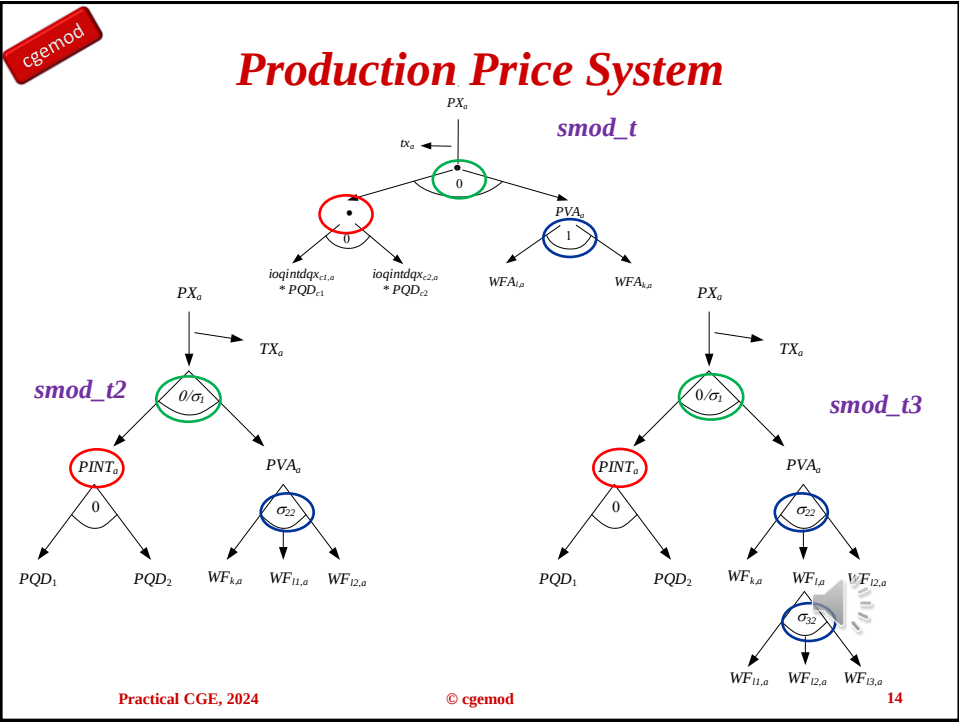
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Method



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$smod_{t2}$ v $smod_t$

- Data
 - Transactions (SAM) data – unchanged
 - Elasticities – add two (ρ_{hox} , ρ_{hova})
- Sets - unchanged
- Equations
 - Nonproduction equations – no change
 - Production equations – change
- Parameters
 - Nonproduction parameters – no change
 - Production parameters – change
- Closures
 - Modify



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smod_t3 v smod_t2

- Data
 - Transactions (SAM) data – changed
 - Elasticities – add three (*rhox*, *rho_{va}*, *rho_{fd}*)
- Sets - extend
- Equations
 - Nonproduction equations – no change
 - Production equations – add another primal and FOC
- Parameters
 - Nonproduction parameters – no change
 - Production parameters – change
- Closures
 - Modify



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Exercises and Experiments



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Exercises and Experiments: smod_t2

- Exercises
 - Coding: revise production system in *smod_t* to make *smod_t2*
 - Test *smod_t2*
- Experiments
 - Trade tax changes with tax replacement
 - As used in ModO5
 - Compare results using *smod_t* and *smod_t2*



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Exercises and Experiments: smod_t3

- Exercises
 - Data: change data used in *smod_t2*
 - Sets: extend sets and add mapping set
 - Coding: revise production system in *smod_t2* to make *smod_t3*
 - Test *smod_t3*
- Experiments
 - Trade tax changes with tax replacement
 - As used in ModO5
 - Compare results using *smod_t2* and *smod_t3*



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Exercises and Experiments: smod_t3_2

- Exercises
 - Data: same data used in *smod_t3*
 - Sets: extend sets and add mapping set
 - Coding: the exogenous data to run a variant of *smod_t3*
 - Test *smod_t3*
- Experiments
 - Trade tax changes with tax replacement
 - As used in ModO5
 - Compare results using variants of *smod_t3*



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The End



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